Essential Elements Math Pacing Guide



January

Background

The Essential Elements Math Pacing Guide was inspired by realizing that there is a small amount of information found on the internet to help support educators who teach those who follow an alternate curriculum for our amazing 1% of the student population in education. I wanted to create something that could help serve as a guide, a support, an understanding of how to hold our students to high academic achievement, just like their regular education peers.

Regular education materials are abundant and come with pacing guides with how to implement the prescribed curriculum that the school decided to buy into. Within those curriculums, a good majority of publishers incorporated how to differentiate Instruction for struggling learners, for English Language Learners and/or English as a Second Language learners. However, there does not seem to be a supplementary curriculum that aligns to how to modify instruction and materials for those who follow the alternate curriculum so the 1% of students with disabilities aligned to the alternate curriculum could also learn a modified version of the same materials as their non-disabled peers in an inclusive setting.

Your partner in education,

Jeanette Nowak

Updated June 2022

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January Outline

Standards covered during January:

- M.EE.6.EE.3 Apply the properties of addition to identify equivalent numerical expressions.
- M.EE.6.EE.5-7 Match an equation to a real-world problem in which variables are used to represent numbers.
- M.EE.7.EE.1 Use the properties of operations as strategies to demonstrate that expressions are equivalent.
- M.EE.8.EE.7 Solve simple algebraic equations with one variable using addition and subtraction.

According to the Dynamic Learning Maps (DLM) website, these are the commonly tested standards that are used for the DLM assessment.

How to Access Math Instruction and Materials from Unique

- 1. https://www.n2y.com/unique-learning-system/
- 2. Log in using the provided username and password you received
- 3. Click on Unique Learning System
- 4. Click on the three lines -----



- 5. Select Monthly Lessons/Unit Lessons
- 6. Select Math
 - a. When selecting materials, select PDF icon to save and print

Understanding Differentiated Levels in Unique

- Level 3 Learners can read text and can participate more independently in the lesson (Independent)
- Level 2 Learners- require pictorial support and require mild to moderate support to participate in the lesson (Supported)
- Level 1 Learners- require extensive supports to participate in the lesson (Participatory).

Measuring Success by the Essential Elements Standards

Students who take DLM assessments are instructed and assessed on *Essential Elements*. Essential Elements are grade-specific expectations about what students with the most significant cognitive disabilities should know and be able to do. The Essential Elements relate to college and career readiness standards for students in the general population.

January Math Pacing Guide 6th Grade

M.EE.6.EE.3 - Apply the properties of addition to identify equivalent numerical expressions.

Learning Goal:

- Level 2-3 Evaluate if equations are true or false.
- Level 1 Students combine and compare sets.

Essential Questions:

- Do the two sides of this problem have equal value?
- Is this expression true (equal) or false (not equal)?

Vocabulary:

- Expression Numbers, symbols and operators (such as + and ×) grouped together that show the value of something.
- **Equal** Exactly the same amount or value.
- Commutative When adding two numbers, the order in which you add them does not matter as the sum will stay the same.
- **Associative** When there are only addition operations within a number sentence, the grouping of the numbers will not matter and the sum will stay the same.



Mini-Map for M.EE.6.EE.3

Subject: Mathematics

Expressions and Equations (EE)

Grade: 6

Learning Outcome

DLM Essential Element	Grade-Level Standard
M.EE.6.EE.3 Apply the properties of addition to identify	M.6.EE.3 Apply the properties of operations to generate
equivalent numerical expressions.	equivalent expressions.

Linkage Level Descriptions

Initial Precursor	Distal Precursor	Proximal Precursor	Target	Successor
Combine two or more sets of objects to form a new set. Compare two or more sets containing objects to communicate	Represent addition or subtraction word problems or models with equations (e.g., 8 marbles + 3 marbles =	Apply commutative (e.g., $3 + 4 = 4 + 3$) and associative [e.g., $2 + (3 + 5) = (2 + 3) + 5$] properties of addition	Create equivalent expressions by applying commutative and associative properties of addition (e.g., the	Recognize or generate an equivalent expression involving addition or subtraction operations using
whether a set has the same, different, or an equal number of objects than the other set.	11 marbles). Recognize that the unknown quantity in an equation is represented using a symbol or letter (e.g., 5 + b = 8).	to add two or more numbers. Evaluate an equation to be true or false by determining whether the numerical value on both sides of an equation is the same or different (e.g., analyze whether 5 + 7 = 8 + 4).	expression 5 + 8 is equal to 8 + 5 due to the commutative property of addition).	commutative and associative properties of addition and multiplication [e.g., recognize that the expression (8 + 6) x 5 is equivalent to 5 x (6 + 8)].

Initial Precursor and Distal Precursor Linkage Level Relationships to the Target

How is the Initial Precursor related to the Target?

Understanding how to evaluate equations and using the properties of addition to create equivalent expressions requires a student to be able to recognize that two or more sets or groups of items exist. Work on this skill using a variety of sets. Help students recognize when items are grouped together into a set or separated out. The educator presents a set, labels it (e.g., two balls, one marker, three CDs), counts the items, labels it again, and encourages students to use numbers to label and count the separate sets. Then, combine the sets, give it a new label, and count the set.

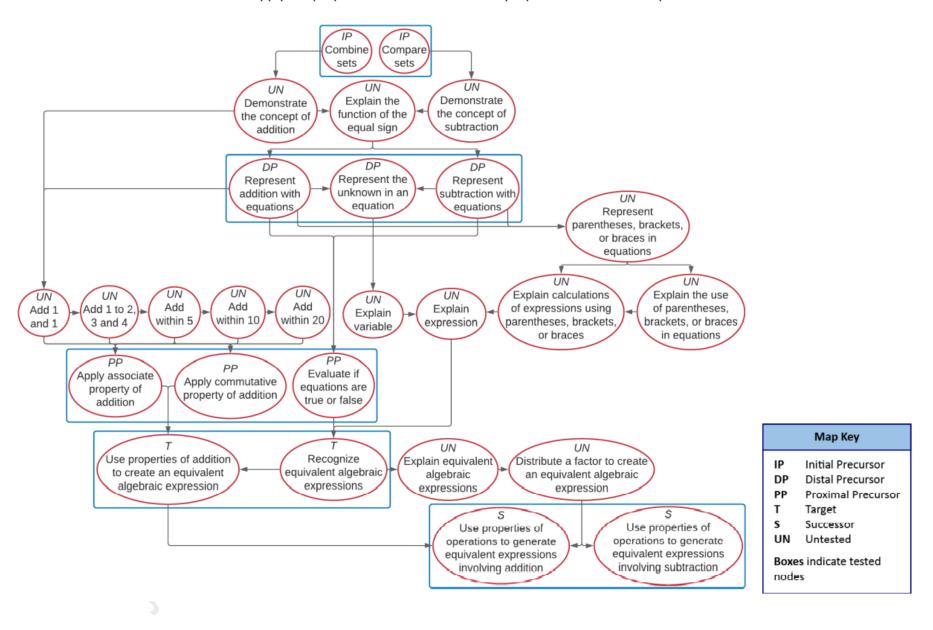
NOTE: Educators can work on the Initial Precursor level using the sets of numbers that students working at the Target level are adding and subtracting.

How is the Distal Precursor related to the Target?

As students begin to understand labeling and counting small sets, they begin to use the number sequence and become more adept at tracking individual objects. Work on this skill using a variety of sets, labeling and counting the sets, and moving items in and out of the sets, labeling and counting the set again. Additionally, the educators will pair those sets with the symbolic representations for addition and subtraction (e.g., 3 + 2 = ?, 3 - 2 = ?).

NOTE: Educators can work on the Distal Precursor level using the sets of numbers that students working at the Target level are adding and subtracting.

M.EE.6.EE.3 Apply the properties of addition to identify equivalent numerical expressions.



Rubric of Student Success

M.EE.6.EE.3 - Apply the properties of addition to identify equivalent numerical expressions.

Level 3 Students will	Level 2 Students will	Level 1 Students will			
Successor and Target Students will	Proximal Precursor and Distal Precursor Students will	Initial Precursor Students will			
Level 3	Level 2	Level 1			
 Evaluate if equations are true or false. 	 Evaluate if equations are true or false. 	• Students combine and compare sets.			
 Successor Use properties of operations to generate equivalent expressions involving subtraction Use properties of operations to generate equivalent expressions involving addition 	 Proximal Precursor Apply associate property of addition Apply commutative property of addition Evaluate if equations are true or false 	Initial Precursor			
 Use properties of addition to create an equivalent algebraic expression Recognize equivalent algebraic expressions 	 Distal Precursor Represent addition with equations Represent the unknown in an equation Represent subtraction with equations 				

Instructional Ideas

M.EE.6.EE.3 - Apply the properties of addition to identify equivalent numerical expressions.

Number sentences and equations show a relationship and can be written in different ways.

The big idea is that a number expression is a math problem that uses numbers and letters to represent variables and an equals sign to show that two quantities have equal value.

- Introduce by asking the essential questions.
- Recognize equivalent algebraic expressions.
- Represent the unknown in the equation.
- Use properties of operation to generate equivalent expressions involving addition, subtraction, multiplication, or division.
- Identify equivalent number sentences.
- Use symbols for equal and not equal.
- Might have to make up your own worksheets but can use the ones provided as inspiration.
- Use manipulatives as needed.
- Students may use a calculator if needed.
- Provide students with their own number line and anchor chart.
- Included worksheets are examples of what to look for when finding additional materials that best fits your student's needs.

Additional Instructional Ideas

- Go to website for additional instructional resources, materials, and activities for lessons:
 - o https://www.msnowakhomeroom.com/3b-equations.html

+	+ Basic Properties of Numbers									
Prop	erty	Explanation	Addition							
Comm	utative	Order doesn't matter	a + b = b + a ex: 1 + 2 = 2 + 1 3 = 3							
Assoc	iative	Grouping doesn't matter	(a + b) + c = a + (b + c) ex: $(2 + 3) + 4 = 2 + (3 + 4)$ 5 + 4 = 2 + 7 9 = 9							

+ Basic Properties of Numbers Commutative Property of Addition a + b = ex: 1 + 2 = a + b = b + b b + b = b + b the equation true?	operty of Addition a + b = b + a
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on equation w ny altogether	ers. to your probler ır equation.	8	Ive the equati ss with the kno he unknown n	В		and B			ther?	Fill in the numbers for ${\bf A}$,	В				then your ans
Write an addition equation wh words: How many altogether?	A and B are known numbers. C is the unknown answer to your problem. Use this model to write your equation.	+	Follow these steps to solve the equation for C. 1. Fill in the empty spaces with the known numbers. Write the variable for the unknown number.	+	+	2. Add the numbers for Aand	A + B		3. C = how many altogether?		+	+		tion true?	quation is true,
+	A and B are C is the unk Use this mod	A	Follow thes 1. Fill in the	A		2. Add the			3. C = how	4. Check your work.	А			Is the equation true?	5. If the eq

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Clues Guide 4 Write and Solve Addition Equations 2

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Yes No					Is the equation true?
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C in the equation. Solve.	C in the	for A, B and	Fill in the numbers for A,	Fill in th	6. Check your work.
			lem.	the prob	5. A = the answer to the problem.
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		for C - B.	emove it. I difference	ing. Re le, A and	4. B - B = 0. 0 = nothing. Remove it. Rewrite the variable, A and difference for C - B .
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uide 5 Name: d Solve Addition Equations 3

Write words
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an addition equation when you see these s: How many **altogether** ?

B is the unknown answer to your problem. are known numbers. and C

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8	low these steps to solve the equation for B. Fill in the empty spaces with the known numbers.
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Write the difference in each space below.

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A - A = 0. 0 = nothing. Remove it. Rewrite the variable, **B** and difference for **C**

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II

В

5. B = the answer to the problem.

6. Check your work. Fill in the numbers for A, B and C in the equation. Solve.

A	+	В	=)	,
	+		=		
			=		
Is the equation true?				Yes	٥N

7. If the equation is true, then your answer for B is correct.

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Addition Properties

Commutative Property of Addition

We can add numbers in any order. Changing the order of the addends doesn't change the sum.

Example:
$$2 + 3 = 3 + 2 = 5$$

Associative Property

how you group the addends, the sum stays the same. We can group numbers in different ways. No matter

Example:
$$(7+6)+4=7+(6+4)=17$$

Identity Property

When we add zero to a number, the sum is the same number.

Example:
$$8 + 0 = 8$$

Inverse Property

When we add a number to its negative, the sum is always zero.

Example:
$$15 + (-15) = 0$$

Name:

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Commutative Property of Addition

Sheet 1

A) Fill in the missing numbers using the commutative property of addition.

$$2) 10+9 = 9$$

$$3) 3+2 = 2$$

$$4) 7+1 = +$$

7

$$6) 4+8 = 8 +$$

1) Which of the following represents the commutative property of addition? B

a)
$$9+7=7+9$$

b)
$$5+1=4+2$$

c)
$$8+3=6+5$$

Which of the following does not represent the commutative property of addition? 5

a)
$$8+6=6+8$$

b)
$$10+2=10+2$$

c)
$$4+5=5+4$$

If 6 + 4 = 10, then 4 + 6 =

Name:

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Associative Property of Addition

Sheet 1

A) Fill in the missing numbers using the associative property of addition.

1)
$$(2+8)+10 = 2+(\underline{}+10)$$
 2) $3+(1+2)$

$$3 + (1 + 2) = (+1) + 2$$

3)
$$(1+3)+9 = 1+(3+$$

4

$$(10+5)+1 = +(5+1)$$

$$5) \quad 2 + (4+5) = (2 + 2) + 5$$

$$7 + (6+1) = (7+6) + _{-}$$

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2) If
$$(10+4)+5=19$$
, then $10+(4+5)=$

Complete the addition equation that represent the associative property. O

1)
$$(3 + 4) + 5 =$$
 + ____ +

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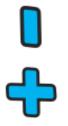
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$$(1 + 2) + 6 =$$
 + 6 = ____

Matching Equivalent Addition and Subtraction Number Sentences

I can correctly match equivalent addition and subtraction number sentences. (ACMNA054)



Draw a line to correctly connect the equivalent addition and subtraction number sentences.

9 - 3 10 - 6 16 - 6	7 - 2	20 - 3	8 - 2
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Balancing Equations:

Addition to 10

Aim: I can balance equations.

Both sides of an equals sign should make the same total.

Work out the answer to the calculation on the left-hand side and write this in both circles. Find the missing number on the right, so the calculation makes the number in the circle.

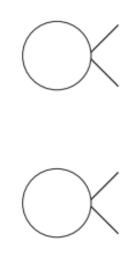
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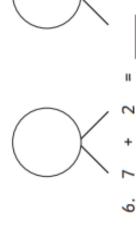
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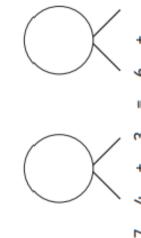






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Balancing Equations: Addition to 10



























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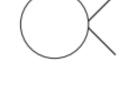


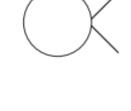






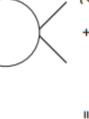


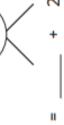


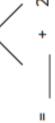


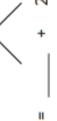
















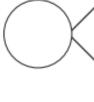




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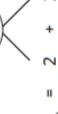


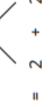






















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Balancing Equations:

Addition to 20

Aim: I can balance equations.

Both sides of an equals sign should make the same total.

Work out the answer to the calculation on the left-hand side and write this in both circles. Find the missing number on the right, so the calculation makes the number in the circle.

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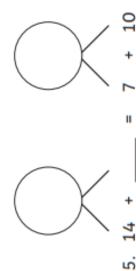


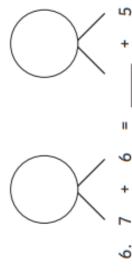
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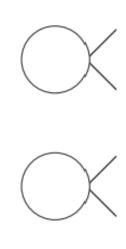
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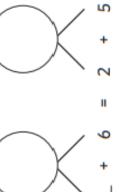




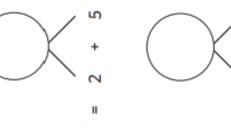
Balancing Equations: Addition to 20











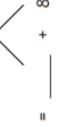






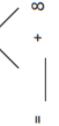








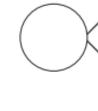


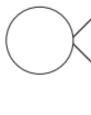


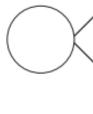




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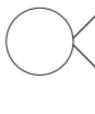












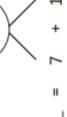




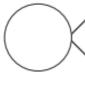


















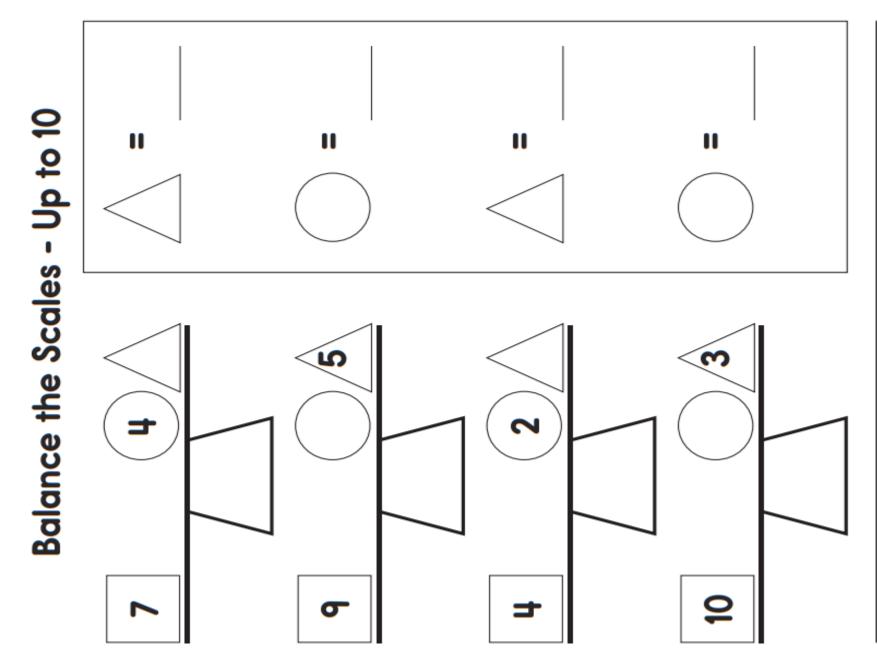
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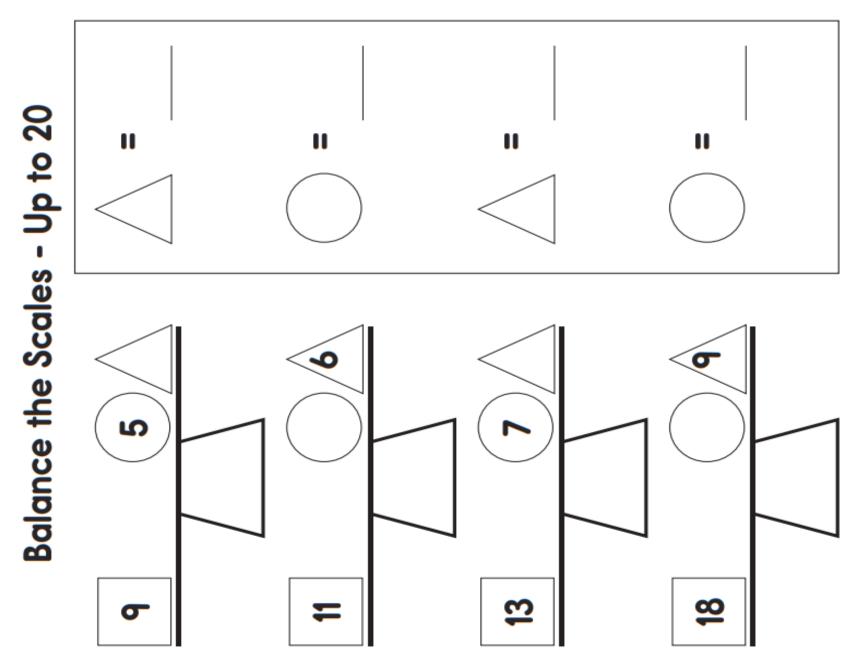
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Finding Unknown Quantities in **Balanced Number Sentences**

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When a number is added to 16, the answer is the same as 8 plus 26. 2

3. When a number is added to 19, the answer is the same as 82 minus 36.

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When a number is subtracted from 91, the answer is the same as 12 plus 6. 4

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5. When a number is subtracted from 88, the answer is the same as 65 plus 9.

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When a number is subtracted from 72, the answer is the same as 59 minus 33. 6.

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7. When a number is added to 61, the answer is the same as 12 plus 74.

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True or False Subtraction Worksheet

Look at the equations. Write the answer for each subtraction and find out if the equations are true or false. Check the correct square box Name_ for each equation.

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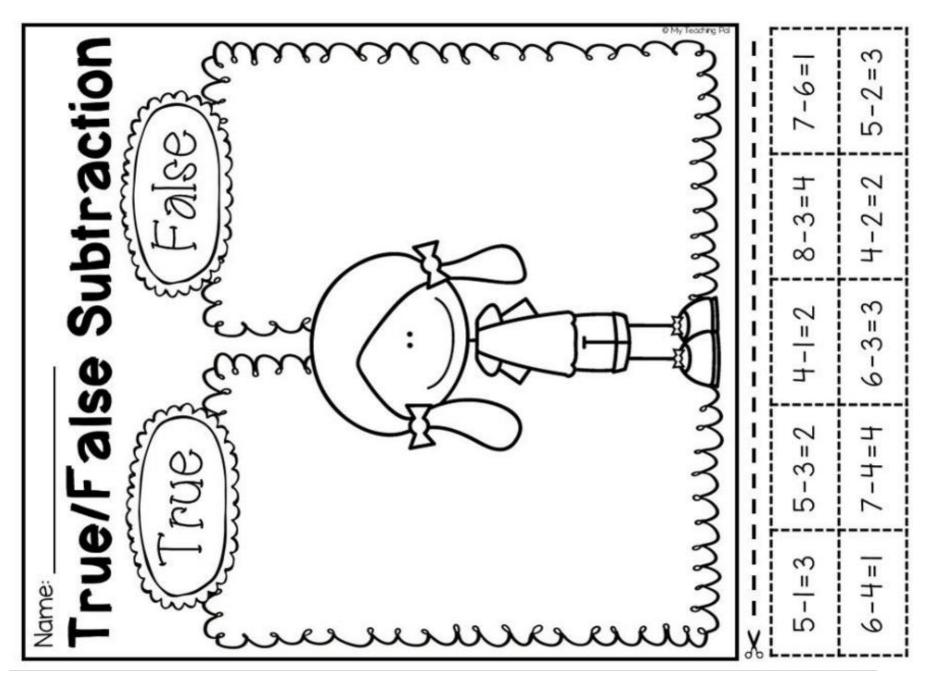
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Name

True or False Addition

Directions: Read the addition equations below. Are they true? Are both sides of the equal sign the same? Fill in the bubbles that show the true equations.

(A) 5+3+1=4+5	A 2+6=4+5 3. B 6+4+1=7+1+3	(A) 8+5=10+3	(A) 3+4=5+2	(A) 2+7=8+1
1. (B) 4+4+2=8+1+2		(B) 12+5=10+3	(B) 9+3=11+2	(B) 12+4=2+4
A 2 + 4 = 4 + 2 Sample Sample	(A) 5 + 5 = 2 + 2 + 3 $(B) 3 + 1 = 2 + 2$	(A)3+3+2=4+4 (B)3+3+3=4+4	(A) 9 + 3 = 3 + 9 (B) 9 + 12 = 8 + 4	(A)8+4=2+5 (B)17+5=5+17

January Math Pacing Guide 6th Grade

M.EE.6.EE.5-7 - Match an equation to a real-world problem in which variables are used to represent numbers.

Learning Goal:

- Level 2-3 Students will represent real-world problems as equations.
- Level 1 Students will combine and partition sets.

Essential Questions:

- What operation is needed in this problem?
- What are the known quantities and the unknown variable in the problem?
- What does the variable represent?
- Which equations matches this problem?

Vocabulary:

- Quantity How much there is of something.
- Variable A symbol for a value we don't know yet. It is usually a letter like x or y.
- Operation A mathematical process with the most common as add, subtract, multiply, and divide (+, -, x, /).



Mini-Map for M.EE.6.EE.5-7

Subject: Mathematics

Expressions and Equations (EE)

Grade: 6

Learning Outcome

DLM Essential Element	Grade-Level Standard
M.EE.6.EE.5-7 Match an equation to a real-world problem in which variables are used to represent numbers.	M.6.EE.5 Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true. M.6.EE.6 Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set. M.6.EE.7 Solve real-world and mathematical problems by writing and solving equations of the form $x + p = q$ and $px = q$ for cases in which p , q and x are all nonnegative rational numbers.

Linkage Level Description

Initial Precursor	Distal Precursor	Proximal Precursor	Target	Successor
Combine two sets of	Represent addition or	Represent expressions	Represent a given real-	Solve real-world
objects to form a new	subtraction word	using variables and	world problem (e.g., Joe	problems with non-
set. Divide objects in a	problems or models	numbers (e.g., express	has 6 markers. Joe has	negative rational
set into two or more	with equations (e.g.,	subtract k from 12 as 12	some crayons. Joe has a	numbers by
subsets.	representing 6 marbles	- k). Recognize that the	total of 10 art supplies.	representing the
	plus 2 marbles equal 8	unknown quantity in an	How many crayons does	situation with a
	marbles as 6 + 2 = 8	equation is represented	Joe have?) with a	mathematical equation
	marbles).	using a symbol or letter	mathematical equation	(e.g., Mark has 3.5
		(e.g., 5 + b = 8).	(e.g., $6 + x = 10$).	

DLM Essential Element: M.EE.6.EE.5-7

Initial Precursor	Distal Precursor	Proximal Precursor	Target	Successor
				inches of string. Mark gets 1 more inch of string. Which equation shows how much string Mark has all together? 3.5 + 1 = x).

Initial Precursor and Distal Precursor Linkage Level Relationships to the Target

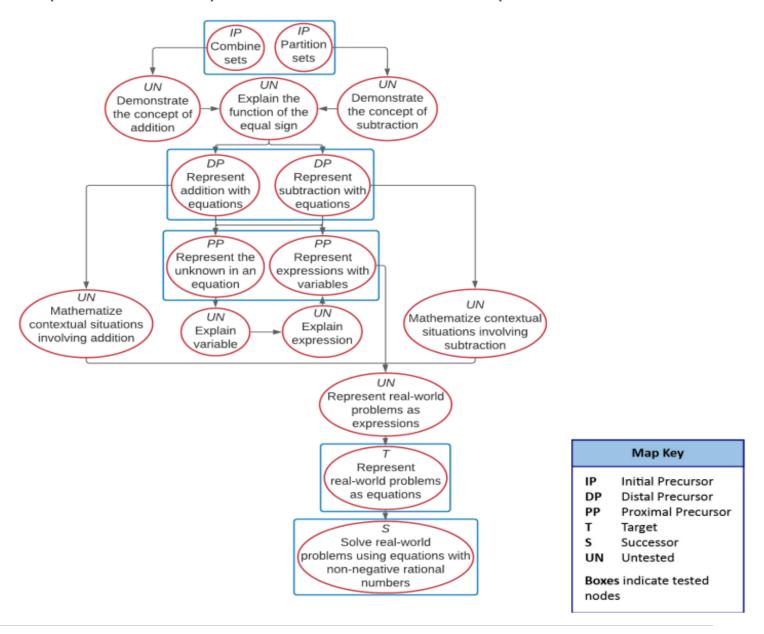
How is the Initial Precursor related to the Target?

The knowledge needed to solve addition and subtraction real-world problems links back to an understanding of how to create sets, but it also requires learning to manipulate sets (i.e., combining and separating or partitioning). Provide students many opportunities to take a set of objects (e.g., tiles, linking cubes, buttons) and separate them based on a given characteristic (e.g., shape, color, size) into two distinct sets, and separate them again based on another characteristic. Guide students to notice how the set size changes each time the educator combines or partitions the sets.

How is the Distal Precursor related to the Target?

As student understanding of combining and partitioning sets increases, educators should take care to use the words "addition" and "subtraction" while defining and demonstrating their meanings and as students combine and partition sets. While students do not need to say the words, they do need to learn the meanings. Educators provide lessons that help students represent addition and subtraction in multiple ways (e.g., using objects, fingers, drawings, sounds, acting out situations, and writing equations).

M.EE.6.EE.5-7 Match an equation to a real-world problem in which variables are used to represent numbers.



Rubric of Student Success

<u>M.EE.6.EE.5-7</u> - Match an equation to a real-world problem in which variables are used to represent numbers.

Level 3 Students will	Level 2 Students will	Level 1 Students will
Successor and Target Students will	Proximal Precursor and Distal Precursor Students will	Initial Precursor Students will
Level 3	Level 2	Level 1
 Students will represent real-world problems as equations. 	Students will represent real-world problems as equations.	Students will combine and partition sets.
Successor • Solve real-world problems using equations with non-negative rational numbers	Proximal Precursor Represent the unknown in an equation Represent expressions with variables	Initial Precursor
TargetRepresent real-world problems as	Mg,	
equations	 Distal Precursor Represent addition with equations Represent subtractions with equations 	

Instructional Ideas

M.EE.6.EE.5-7 - Match an equation to a real-world problem in which variables are used to represent numbers.

Mathematical situations and structures can be translated and represented abstractly using variables, expressions, and equations.

The big idea is that letters are used in mathematics to represent generalized properties, unknowns in equations, and relationships between quantities.

- Introduce by asking the essential questions.
- Identify what operation is needed in the real-world problem.
- Identify the known quantities and the unknown variable.
- Identify the structure of the equation.
- Match an equation to a real-world problem.
- Use manipulatives as needed.
- Students may use a calculator if needed.
- Included worksheets are examples of what to look for when finding additional materials that best fits your student's needs.

Additional Instructional Ideas

• Go to website for additional instructional resources, materials, and activities for lessons:

Solving Linear Equations With an Unknown on One Side

numbers (constants) on the other. You are only able to cancel one term or Your goal is to get the variable on one side of the equals sign and the number at a time and you must use its inverse when canceling.

$$a + 4 = 12$$

Solving Linear Equations With an Unknown on One Side

numbers (constants) on the other. You are only able to cancel one term or Your goal is to get the variable on one side of the equals sign and the number at a time and you must use its inverse when canceling.

$$a + 4 = 12$$

$$a = 8$$

Numerical Expressions Matching Game

Arthur saw three times as many red birds as blue birds (b).

How many red birds did he see?

Salim read 15 pages of a book each day for (p) days.

How many pages did she read in total? Leila painted 6 pictures. Each one took her (t) minutes to paint.

How long did she paint for?

Judith baked 4 pies and gave away (p) pies.

How many were left?

Luca had 45 crayons and split them into (n) equal groups. How many were in each group?

Kamal ran half as many miles on Tuesday as Monday (m).

How many miles did he run on Tuesday? Javonte and Lola shared (q) candies equally.

How many did they get each?

Min practiced piano for 45 minutes on Monday. She practiced (r) minutes longer on Tuesday.

How many minutes was this?

Yasir did his homework yesterday for (y) minutes. It will take him twice as long to finish it tonight.

How long is that?

Rida bought 4 packs of highlighters with (h) highlighters in each pack.

How many altogether?

Numerical Expressions Matching Game

45 + n

4 × h

× × 2

Q

× 9

45

q + 2

2

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15 × p

15

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Numerical Expressions Matching Game Answers

Arthur saw three times as many red birds as blue birds (b). Hows many red birds did he see?

Kamal ran half as many miles on Tuesday as Monday (m). How many miles did he run on Tuesday?

Judith baked 4 pies and gave away (p) pies. How many were left?

4

Min practiced piano for 45 minutes on Monday. She practiced (r) minutes longer on Tuesday. How many

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Luca had 45 crayons and split them into (n) equal groups. How many were in each group? ŝ

Rida bought 4 packs of highlighters with (h) highlighters in each pack. How many altogether? ø

Yasir did his homework yesterday for (y) minutes. It will take him twice as long to finish it tonight. How 7

Leila painted 6 pictures. Each one took her (t) minutes to paint. How long did she paint for?

ထ

Javonte and Lola shared (q) candies equally. How many did they get each? o.

Salim read 15 pages of a book each day for (p) days. How many pages did she read in total? <u>0</u>

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) Natalie buys organic almonds priced at \$77 from the grocery store. How much did she pay the cashier, if she received \$23 in change?	.) Lara and Mae participated in a quiz contest. They scored 23 points in all. If Lara scored 9 points, how many points did Mae score?	John was gifted a pack of crayons. He gave 13 crayons to his friend Rhea and was left with 11 crayons. How many crayons did the pack contain?	Smith and his friends are gaming online on a popular website. An hour later, 6 friends go offline. Five of them continue playing. How many of them were gaming online initially?	Trevor takes up a test at school and completes it in an hour. The test has two sections. If he takes 35 minutes to complete the first section, how much time does he have left to complete the second section?	
=	2)	3)	4	5)	

One-Step Equations - Integers

Add/Sub: S1

Natalie buys organic almonds priced at \$77 from the grocery store. How much did she pay the cashier, if she received \$23 in change? 7

x - 77 = 23;\$100

Lara and Mae participated in a quiz contest. They scored 23 points in all. If Lara scored 9 points, how many points did Mae score? 2)

x + 9 = 23; 14 points

John was gifted a pack of crayons. He gave 13 crayons to his friend Rhea and was left with 11 crayons. How many crayons did the pack contain? 3

x - 13 = 11; 24 crayons

Smith and his friends are gaming online on a popular website. An hour later, 6 friends go offline. Five of them continue playing. How many of them were gaming online initially? 4

x - 6 = 5; 11 persons

sections. If he takes 35 minutes to complete the first section, how much time does Trevor takes up a test at school and completes it in an hour. The test has two he have left to complete the second section? 2

x + 35 = 60;25 minutes

			=u		
5 ке	isha fill	s 5 wa	Keisha fills 5 water bottles.		a
n	ındy fills	s n wai	Randy fills n water bottles.		
ф 6	ey fill 9	water	They fill 9 water bottles altogether.		
Write an equation. Solve for n to find	uation. to find	out ho	Write an equation. Solve for n to find out how many water bottles Randy fills.	s Ran	dy fills.
		+	u	=	
	ı	+		=	
•		+	n	=	-
·		+		=	 -
		+		=	
			n	=	
Since n =	, ,	, Randy fills	ills water bottles.	tles.	

Raj stacks 4 fishing poles.

4

Mary Beth stacks n fishing poles.



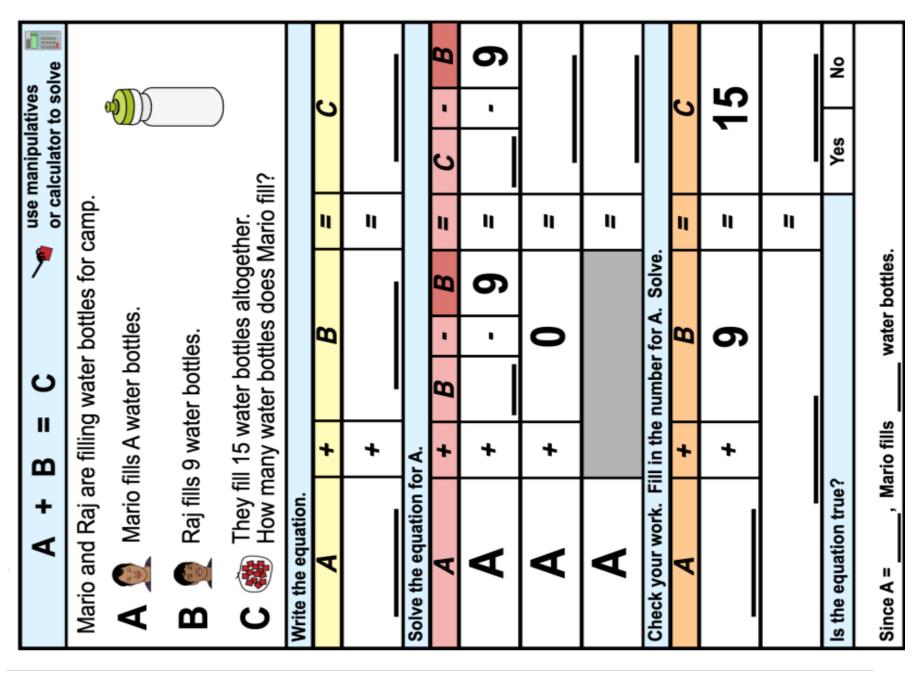
Solve for n to find out how many fishing poles Mary Beth stacks. They stack 12 fishing poles altogether. Write an equation.

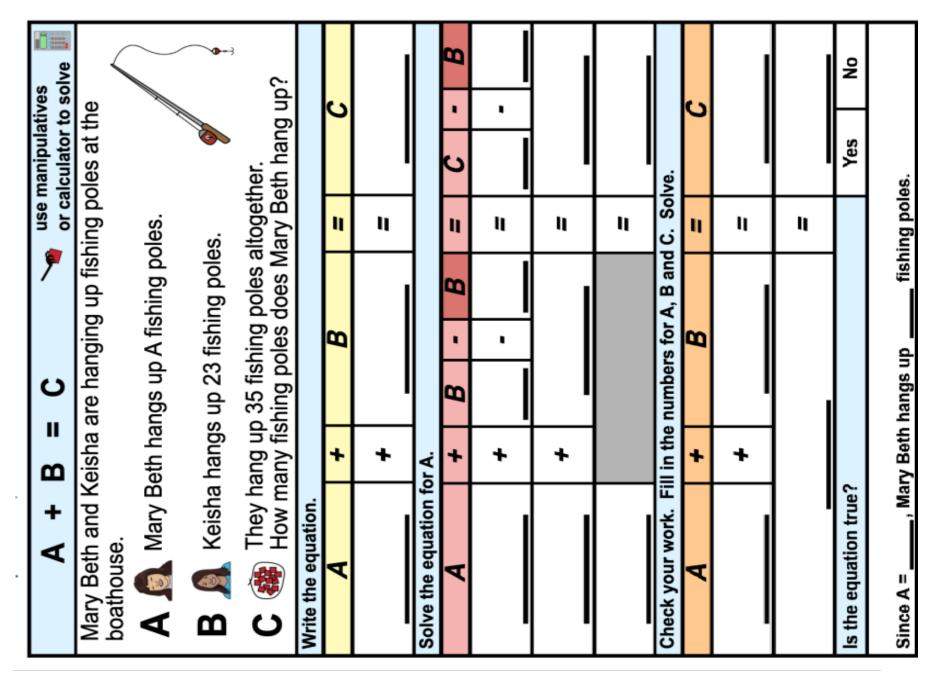
Dott Stacks.			•	 - 			
2	=	=	=	=	=	=	
Solve for it to find out flow finding holes fridly bett stated.	u		u			u	
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fishing poles.

, Mary Beth stacks

Since n =





A and C are known numbers. B is th Use this model to write your equation. A and C are known numbers. B is th Use this model to write your equation. A the empty spaces with the kn Write the variable for the unknown A + + + C. Subtract the number for A from bot A + + A - A + +	are known numbers. are known numbers. ase steps to solve the second the empty spaces with the variable for the under the number for Africat the number for Afr	te your can be you	e unknown are unknown are unknown are unknown are nown number. B B B B B B B B B B B B B	nswer to yo	your probl	i o
3. Write the difference in each space	e differenc	e in eac	۵	lı		$\dashv \vdash \vdash$
4. A - A= (Rewrite	0. 0 = noth the variab	ning. Rele, B and	A - A= 0. 0 = nothing. Remove it. Rewrite the variable, B and difference for C - A. B	п		
5. B = the a	B = the answer to the problem. Check your work. Fill in the nu	the prot	mbers for A,	B and C in the	e equation.	. Solve.
		+	В	=		
		+		=		
				=		
Is the equation true?	tion true?				Yes	N N
7. If the equation is true	t si uciter i		then volir answer for B is correct	orract		

■ Write	a subtrac	tion equ	ation v man	when yo	u see ti han? H	Write a subtraction equation when you see these words: How many are left? How many more than?	s: ess than?
B and C are known numbers. A is th Use this model to write your equation.	are known numbers. nodel to write your ed	s. A is the	e unk	nown an	swer to	A is the unknown answer to your problem. uation.	m.
А	•		В		=)	S
Follow these steps to solve the equation for A. 1. Fill in the empty spaces with the known numbers. Write the variable for the unknown number.	s to solve / spaces w ile for the u	the equainth the kranknown	ation f lown r numb	or A. numbers. er.			
A	•		В		=)	C
A	٠				=		
2. Since B is negative,		add the number for B to both sides	er for	3 to both	sides o	of the equal sign	sign.
A		В-	+	В	=	C	+ B
A			+		=		+
3. Write the sum in	sum in each space below.	ice below]				
A					=		
 4B + B = 0. 0 = nothing. Remove it. Rewrite only the variable, A and sum for C + B 	0 = nothing. F / the variable,	Remove it. Aand sun	t. m for	C + B			
A					=		
5. A = the answer to the problem.	to the prok	olem.					
6. Check your work.		Fill in the numbers for A,	ers for		C in th	B and C in the equation.	Solve.
А	-		В		=)	S
	•				=		
					=		
Is the equation true?	le?					Yes	No
7. If the equation is true, then your answer for A is correct.	s true, the	n your an	swer 1	or Ais co	orrect.		

B ŝ or calculator to solve use manipulatives Mario hands out 12 more life jackets than Raj. Yes How many life jackets does Mario hand out? Mario and Raj are handing out life jackets at camp. Remember that B is negative II II II П II II II П life jackets. Solve. Mario hands out A life jackets. Raj hands out 20 life jackets. മ Fill in the number for A. 20 B 8 , Mario hands out ပ **-B** Ш Solve the equation for A. മ Is the equation true? Check your work. ⋖ ⋖ ◂ Since A = മ

January Math Pacing Guide 7th Grade

M.EE.7.EE.1 - Use the properties of operations as strategies to demonstrate that expressions are equivalent.

*** Please refer to the December pacing guide as it has the standard and additional materials.

January Math Pacing Guide 8th Grade

M.EE.8.EE.7 - Solve simple algebraic equations with one variable using addition and subtraction.

Learning Goal:

- Level 2-3 Solve linear equations in one variable.
- Level 1 Combine and partition sets.

Essential Questions:

- What am I trying to figure out in this equation?
- What do I know about the properties of addition and subtraction that can help me solve this problem?

Vocabulary:

• Variable – A symbol for a value we don't know yet. It is usually a letter x or y.



Mini-Map for M.EE.8.EE.7

Subject: Mathematics

Expressions and Equations (EE)

Grade: 8

Learning Outcome

DLM Essential Element	Grade-Level Standard
M.EE.8.EE.7 Solve simple algebraic equations with one variable	M.8.EE.7 Solve linear equations in one variable.
using addition and subtraction.	

Linkage Level Descriptions

Initial Precursor	Distal Precursor	Proximal Precursor	Target	Successor
Combine two or more sets of objects or numbers to form a new set. Split one set into multiple sets grouped together by similar	Demonstrate understanding of addition by combining the objects of two or more sets and demonstrate	Determine the unknown/missing addend (e.g., 8 + x = 12) or sum (e.g., 4 + 6 = x) when given an equation with addition operation	Solve linear equations involving addition, subtraction, multiplication, or division operations in one variable (e.g., 8.4 +	Solve linear inequalities in one variable (e.g., 6 < 8 + x).
characteristics.	understanding of subtraction by removing some objects from a larger set.	and determine the unknown/missing minuend or subtrahend (e.g., 9 - x = 16) or the difference (e.g., 13 - 5 = x) when given an equation with subtraction operation.	x = 17.56).	

Initial Precursor and Distal Precursor Linkage Level Relationships to the Target

How is the Initial Precursor related to the Target?

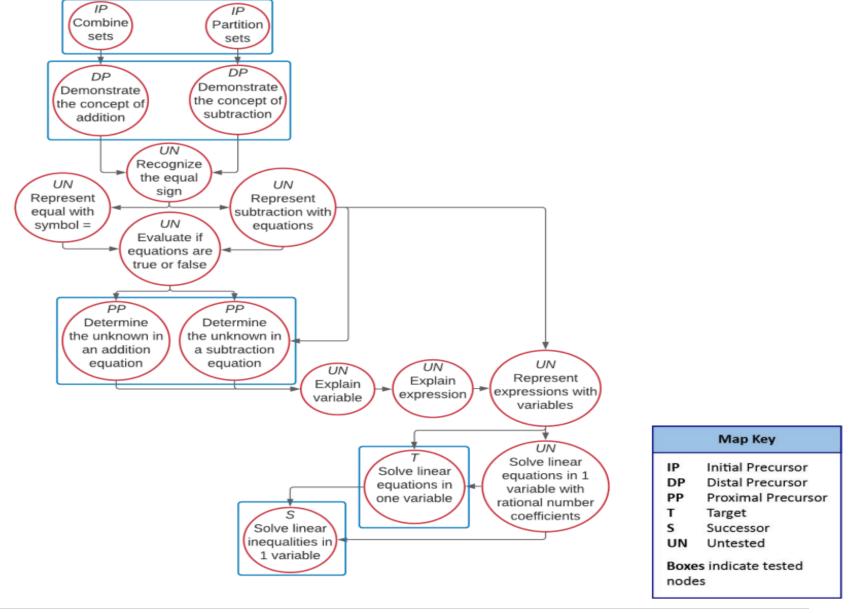
Solving linear equations requires a student to count small units, recognizing that two or more sets or groups of items exist. Work on this skill using a variety of sets. Help students recognize when items are grouped together into a set or separated out. The educator presents a set, labels it (e.g., two balls, one marker, three CDs), counts the items, labels it again, and encourages students to use numbers to label and count the separate sets. The general goal is to explore how the set changes when items are separated out (partitioned) or combined.

How is the Distal Precursor related to the Target?

As students begin to understand labeling and counting small sets, they begin to use the number sequence and become more adept at tracking individual objects. They can recognize when items are added to a set or when items are taken away. Work on this skill using a variety of sets, labeling and counting the set, and moving items in and out of the set, labeling and counting the set again.

NOTE: Educators can work on the Distal Precursor level using the sets of numbers that students working at the Target level are working with.

M.EE.8.EE.7 Solve simple algebraic equations with one variable using addition and subtraction.



Rubric of Student Success

<u>M.EE.8.EE.7</u> - Solve simple algebraic equations with one variable using addition and subtraction.

Level 3 Students will	Level 2 Students will	Level 1 Students will
Successor and Target Students will	Proximal Precursor and Distal Precursor Students will	Initial Precursor Students will
Level 3 • Solve linear equations in one variable.	Level 2 • Solve linear equations in one variable.	Level 1 • Combine and partition sets.
Successor • Solve linear inequalities in 1 variable Target • Solve linear equations in one variable	 Proximal Precursor Determine the unknown in an addition equation Determine the unknown in a subtraction problem Distal Precursor Demonstrate the concept of addition Demonstrate the concept of subtraction 	Initial Precursor

Instructional Ideas

M.EE.8.EE.7 - Solve simple algebraic equations with one variable using addition and subtraction.

Equations express a relationship that can be used to solve an unknown.

The big idea is that variables represent the unknown in an equation.

- Introduce by asking the essential questions.
- Determine the unknown in an equation.
- Use property of inverse operation (addition/subtraction) to complete the inverse to each side of the equation.
- Isolate the variable to solve.
- Solve algebraic expressions using addition or subtraction.
- Use manipulatives as needed.
- Students may use a calculator if needed.
- Included worksheets are examples of what to look for when finding additional materials that best fits your student's needs.

Additional Instructional Ideas

• Go to website for additional instructional resources, materials, and activities for lessons:

Clues Write

Clues Guide 4 Write and Solve Addition Equations 2

Write an addition equation when you see these words: How many altogether?

B and C are known numbers. A is the unknown answer to your problem. Use this model to write your equation.	numbers ite your	s. A is the	ne unk	nown an	swer to	your proble	Ë.
А	+		В		=)	2
Follow these steps to solve the equation for A. 1. Fill in the empty spaces with the known numbers Write the variable for the unknown number.	o solve paces w for the u	the equaith the krainknown	ation 1 nown r numb	f or A. numbers. er.			
А	+		В		=)	S
A	+				=		
2. Subtract the number for B from both sides of the equal sign.	er for B	from bot	th side	s of the	equal sig	gn.	
А	+	В	•	В	=	3	- B
A	+		-		=		_
3. Write the difference in each space below.	e in eac	h space	below				
A	+				П		
4. B - B = 0. 0 = nothing. Remove it. Rewrite the variable, A and difference for C - B	hing. Re ile, A an	emove it. d differer	ce for	C-B			
A					=		
5. A = the answer to the problem.	the prob	lem.					
6. Check your work.	Fill in th	Fill in the numbers for A,	ers for		C in th	B and C in the equation.	Solve.
Α	+		В		=)	S
	+				=		
					=		
Is the equation true?						səД	N
7. If the equation is true, then your answer for A is correct.	rue, ther	your an	swer	for A is co	orrect.		

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/	1
0	10
(A)	2
1	1
	-

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Suide 5 Name: nd Solve Addition Equations 3

Write an a
+

addition equation when you see these low many altogether?

are known numbers. B is the unknown answer to your problem. A and C are known numbers. B is the Use this model to write your equation.

3	
=	
В	e steps to solve the equation for B.
+	solve
А	hes
	ow t

Folk

Fill in the empty spaces with the known numbers.
 Write the variable for the unknown number.

А	+	8	=	\mathcal{C}
	+	8	=	

Subtract the number for A from both sides of the equal sign.

	Y		
	-	-	
0	C		
	=	=	
	8	Я	
	+	+	
	Α		
	•	-	
	Α		

Write the difference in each space below.

II Ø

A - **A**= 0. 0 = nothing. Remove it. Rewrite the variable, **B** and difference for **C**

4

II В

5. B = the answer to the problem.

6. Check your work. Fill in the numbers for A, B and C in the equation. Solve.

А	+	8	=)	,
	+		=		
			=		
Is the equation true?				ХeУ	ON

7. If the equation is true, then your answer for B is correct.

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Clues Guide 7 Verite and Solve Subtraction Equations 2

Write a	Write a subtraction equation when you see these words: How many are left? How many more than? How many less than?	tion equ	ation v man	when yo	ou see t	hese wo	rds: v less	than?
B and C are known numbers. A is th Use this model to write your equation.	number rite your	s. A is the	ie unk	nown an	swer to	A is the unknown answer to your problem. uation.	blem.	
Α	•		В		=		ပ	
Follow these steps to solve the equation for A. 1. Fill in the empty spaces with the known numbers. Write the variable for the unknown number.	to solve spaces we for the u	the equainth the kname	ation i	for A. numbers. er.				
A	-		В		=		ပ	
¥	٠				П			
2. Since B is negative,	ve, add the	he numbe	er for	number for B to both sides of the	sides o		equal sign	٠
A		В-	+	8	=	2	+	В
Ą			+		н		+	
3. Write the sum in each space below.	each spa	ce below						
A					=			
4B + B = 0. 0 = nothing. Remove it. Rewrite only the variable, A and sum for C + B	0 = nothing. F / the variable,	Remove it Aand sun	t. m for	C + B				
٨					=			
5. A = the answer to the problem.	the prok	olem.						
6. Check your work.		Fill in the numbers for A,	ers for	B	and C in the	e equation.		Solve.
Α	_		В		=		S	
	•				=			
					=			
Is the equation true?	ن					Yes		N _o
7. If the equation is true, then your answer for A is correct	true, the	n vour an	swer	for A is co	orrect.		-	

Clues Guide 8 Write and Solve Subtraction Equations 3

•	Write a s How ma	subtract ny are le	tion equa	r tion man	when yo y more t	nu see t han? H	Write a subtraction equation when you see these words: How many are left? How many more than? How many less than?	s: ss than?
A and C SUS	A and C are known numbers. B is th Use this model to write your equation.	numbers te your	s. B is the	yun e	nown an	swer to	B is the unknown answer to your problem uation.	m.
A	1	•		В		=)	S
Follow the 1. Fill in the	Follow these steps to solve the equation for B. 1. Fill in the empty spaces with the known numbers Write the variable for the unknown number.	o solve paces wi for the u	the equalith the known responsible.	tion 1 own r dmbr	f or B. numbers. er.			
_	A	·		В		=)	;
		-		В		=		
2. Subtra	Subtract the number for	er for A	A from both sides of the	side	s of the e	equal sign.	Jn.	
Α.	Y .	-		В		=	. 3	Α .
_		•		В		=	·	_
3. Write the	3. Write the difference in each space below.	e in eac	h space b	oelow				
		٠		В		=		
4. A - A = 0 of C - A.	 0. 0 = nothing. Remove it. Rewrith. Notice that B is now a negative B. 	ning. Re at B is n	move it. ow a nega	Rewr ative	ite the va B.	ariable,	Rewrite the variable, B and difference ative B .	ence
				-B		=		
5. Multiply	5. Multiply -1 to each side	side of	of the equal		sign to make	⊭	a positive B .	
			1-	X	-В	=	x 1-	(C - A)
				В		=		
6. B = the	B = the answer to the problem.	the prob	olem.					
7. Check	Check your work.	Fill in th	Fill in the numbers for A,	rs for	A, B and	C in th	C in the equation.	Solve.
A	1	-		В		=)	;
		-				=		
						=		
Is the equ	Is the equation true?						Yes	ON
8. If the e	8. If the equation is true, then your answer for B is correct.	rue, ther	your ans	swer i	for B is c	orrect.		

65 | Page

Name:

One-Step Equations: Integers

Add/Sub Level 1

Solve each equation.

1)
$$x + 9 = 12$$

2)
$$s-1=10$$

3)
$$3 = z - 11$$

4)
$$5+y=7$$

5)
$$8 = 2 + q$$

$$6 = n - 4$$

9

7)
$$r-2=5$$

$$9 + m = 9$$

8

$$p + 7 = 8$$

6

10)
$$4+a=13$$

Date Name

Solve One-Step Addition and Subtraction Equations

You can solve one-step equations using inverse operations. For example, addition and subtraction are inverse operations. To solve a one-step addition or subtraction equation, apply the inverse operation to both sides of the equation to get the variable alone.

Let's try it! Solve each equation.

$$n + 5 = 16$$

$$n+5-5=16-5$$
 Subtract 5 from both sides of the equation.
 $n=11$

$$b - 4 = 13$$

4

b - 4 + 4 = 13

b = 17

Try it yourself! Solve each equation.

ĸ,

$$v + 9 = 23$$

$$7 + c = 22$$

5

4.

6

21 = 16

$$11 + x = 35$$

Ν,

$$k - 15 = 28$$

ထ

$$z + 14 = 27$$

6

$$f - 17 = 24$$

6

$$26 + m = 32$$

Ξ.

$$m = 32$$

$$d - 25 = 39$$

7

$$28 + s = 57$$

13

$$u - 21 = 0$$

4.

$$-21 = 29$$

$$y + 33 = 76$$

<u>1</u>



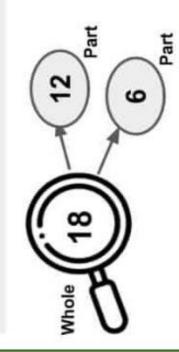
Helping With Math

Determining the Unknown Whole Number in an Addition or Subtraction Equation





and subtraction equation, we must understand the correlation of addition addition In determining the unknown whole number in an and subtraction as part of a whole.





- number is called The biggest the whole.
- numbers are its The other two parts.

Adding the parts gives the

whole.

6 + 12 = 1812 + 6 = 18

12 = 6

18 - 6 = 12







Addition or Subtraction Equation Determining the Unknown



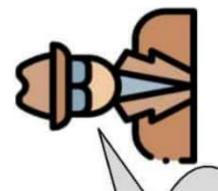
Finding the Missing Whole or Missing Part

Sometimes, we may have problems like these:





ω II



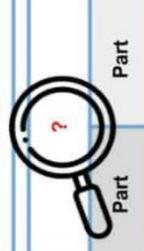
How can we find these missing numbers? We can find these missing numbers in the equations using whole and parts.

Part-Part-Whole Model

Whole

Part

Part



Part Mhole

Missing Part: Subtract Part = Whole - Part

Missing Whole: Add Whole = Part + Part Determining the Unknown Whole Number in an Addition or Subtraction Equation



Finding the Missing Minuends and Subtrahends

subtract the difference from the minuend If the unknown number is the subtrahend, (number before the minus sign)

$$15 - 11 = 4$$

Therefore, the unknown number is 4.

$$15 - ? = 11$$

If the unknown number is the minuend, simply add the two known numbers.

$$5 + 8 = 13$$

herefore, the unknown number is 13.

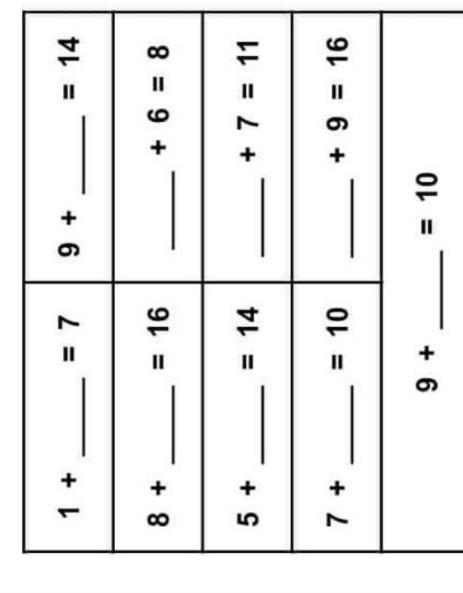
$$9 - 5 = 8$$

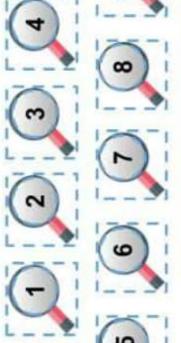
Determining the Unknown Whole Number in an Addition or Subtraction Equation



THE CLUES

Cut out the clues below and fill in the missing addends to complete each equation.





Determining the Unknown Whole Number in an Addition or Subtraction Equation

MASTER TRAINING

linear equations

addition

solve.

$$x = \frac{-21}{}$$

$$2. -7 = x + 9$$

1. -18 =) -18 =) -3 -21 =)

4. -22 + x = -4

$$6. x + 5 = -15 x =$$

5. -15 + x = 24

$$8. x + 10 = -1$$

9.
$$-7 + x = -12$$
 x

$$10. -9 = x + 6$$

TRAINING COMPLETE

More worksheets at www.education.com/worksheets



Complete the following algebra equations.

Remember: what you do to one side of the equation, you have to do to the other side.

$$ex.$$
 1. x + 10 = 32

2.8 + x =

$$x + 10 - 10 = 32 - 0$$

 $x = 27$

$$3. x - 7 = 20$$

$$4. x - 9 = 17$$

$$5.19 + x = 2$$

$$6.x + 7 = 44$$

$$7.2x + 5 = 15$$



Credits

Websites Used for Worksheets and Lesson Ideas:

- https://www.education.com
- https://www.twinkl.com
- https://www.superteacherworksheets.com
- https://www.easyteacherworksheets.com
- https://www.mathworksheets4kids.com
- https://www.math-salamanders.com
- https://www.math-drills.com
- https://www.mathsisfun.com/definitions/index.html

Resources Used to Help Create the Pacing Guide:

DLM Essential Elements Unpacking

• https://www.dlmpd.com/dlm-essential-elements-unpacking

Instructional Resources for YE Model States

• https://dynamiclearningmaps.org/instructional-resources-ye/mathematics

Dynamic Learning Maps

• https://dynamiclearningmaps.org

Unique Learning System

• https://www.n2y.com/unique-learning-system

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